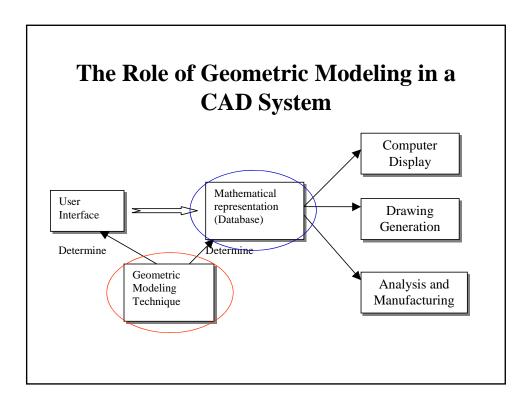
Geometric Modeling



Introduction

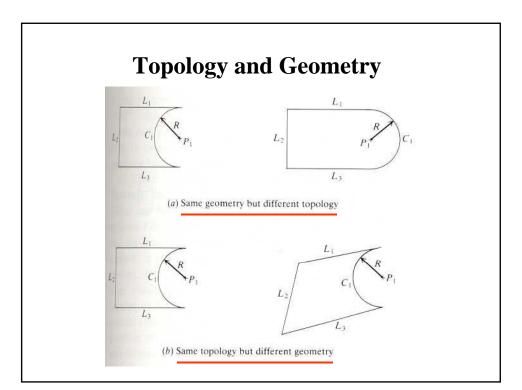
"Geometric modeling is as important to CAD as governing equilibrium equations to classical engineering fields as mechanics and thermal fluids."

- ✓intelligent decision on the types of entities necessary to use in a particular model to meet certain geometric requirements such as slopes and/or curvatures.
- ✓interpretation of unexpected results
- ✓ evaluations of CAD/CAM systems
- ✓innovative use of the tools in particular applications.
- ✓ creation of new attributes, or modify the obtained models to benefit new engineering applications.
- ✓ understanding of terminology



General Requirements

- Complete part representation including topological and geometrical data
 - Geometry: shape and dimensions
 - Topology: the connectivity and associativity of the object entities; it determines the relational information between object entities
- Able to transfer data directly from CAD to CAE and CAM.
- Support various engineering applications, such as mass properties, mechanism analysis, FEA/FEM and tool path creation for CNC, and so on.



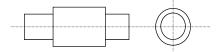
Comments on Geometric Modeling

- Geometric modeling is only a means not the goal in engineering.
- Engineering analysis needs product geometry; the degree of detail depends on the analysis procedure that utilizes the geometry.
- There is <u>no</u> model that is <u>sufficient</u> to study all behavioral aspects of an engineering component or a system.
- Attributes facilitate analysis and grow with applications

Basic Geometric Modeling Techniques

- 2-D Projection (Drawings)
- Wireframe Modeling
- Surface Modeling
 - Analytical Surface
 - Free-form, Curved, & Sculptured Surface
- Solid Modeling
 - Constructive Solid Geometry (CSG)
 - Boundary Representation (B-Rep)
 - ..
 - Feature Based Modeling
 - Parametric Modeling

2-D Projection



Problems:

- Training is necessary to understand the drawing
- Mistakes often occur
- Does not support subsequent applications such as finite element analysis (FEA) or NC part programming

Wireframe Modeling

- Developed in 1960s and referred as "a stick figure" or "an edge representation"
- The word "wireframe" is related to the fact that one may imagine a wire that is bent to follow the object edges to generate a model
- Model consists entirely of <u>points</u>, <u>lines</u>, <u>arcs</u> and <u>circles</u>, <u>conics</u>, and curves.
- In 3D wireframe model, an object is not recorded as a solid.
 Instead the vertices that define the boundary of the object, or the intersections of the edges of the object boundary are recorded as a collection of points and their connectivity.









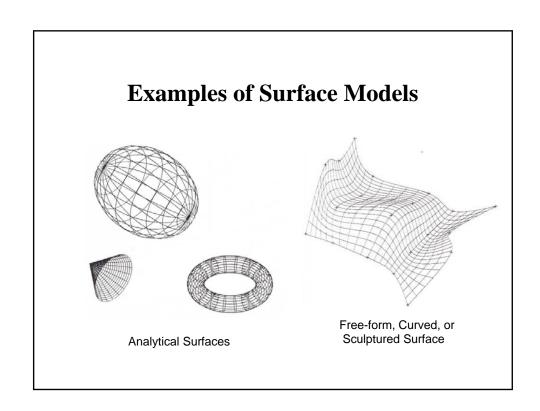
ambiguous

Example of Wireframe Modeling Top view Isometric view Right view

Surface Modeling

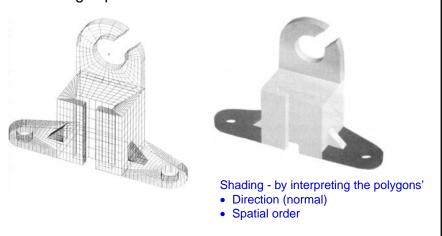


- A surface model is a set of faces.
- A surface model consists of <u>wireframe</u> entities that form the basis to create surface entities.
- In general, a <u>wireframe model</u> can be extracted from a <u>surface model</u> by <u>deleting or blanking all surface entities</u>
- Shape design and representation of complex objects such as car, ship, and airplane bodies as well as castings
- Used to be separated, <u>shape model</u> are now incorporated into <u>solid models</u> (e.g. Pro/E)



Examples of Surface Models

- Surface models define only the geometry, no topology.
- Shading is possible





Solid Modeling

- The solid modeling technique is based upon the "half-space" concept.
- The boundary of the model separates the interior and exterior of the modeled object.
- The object is defined by the <u>volume space contained within the defined boundary of the object</u>.
- In general speaking, a closed boundary is needed to define a solid object.
- informationally complete, valid, and unambiguous representation (Spatial addressability)
 - points in space to be classified relative to the object, if it is inside, outside, or on the object
- store **both geometric and topological** information; can verify whether two objects occupy the same space.
- improves the quality of design, improves visualization, and has potential for functional automation and integration.

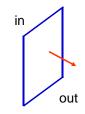
Why Solid Modeling?



Solid Modeling Support

- Using volume information
 - weight or volume calculation, centroids, moments of inertia calculation,
 - stress analysis (finite elements analysis), heat conduction calculations, dynamic analysis,
 - system dynamics analysis
- Using volume and boundary information
 - generation of CNC codes, and robotic and assembly simulation

Foundation of SOLID Modeling (Element of Primitives): Half Space



- Unbounded geometric entities
- Each one of them divides the representation space into infinite portions, one filled with material and the other empty
- Surfaces can be considered half-space boundaries and half spaces can be considered <u>directed</u> surfaces
- An object is defined by the volume space contained within the defined boundary of the object

Introduces the direction into the modeling, thus enables the topological information be stored in a geometric model

Half Spaces



- By specifying different boundary surface, we can have any half-spaces;
- The most commonly used half-spaces are
 - planar, cylindrical, spherical, conical, and toroidal.
- By combining half-spaces (using Boolean operations) in a building block fashion, various solids can be constructed.

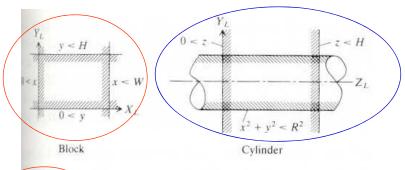
Half Spaces

Planar half-space

$$H = \{(x, y, z) : z < 0\}$$

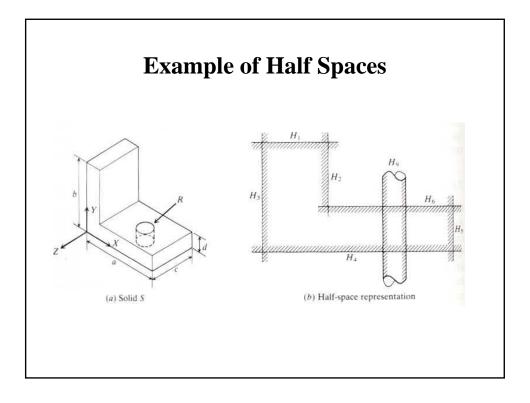
• Cylindrical half-space

$$H = \{(x, y, z) : x^2 + y^2 < R^2\}$$



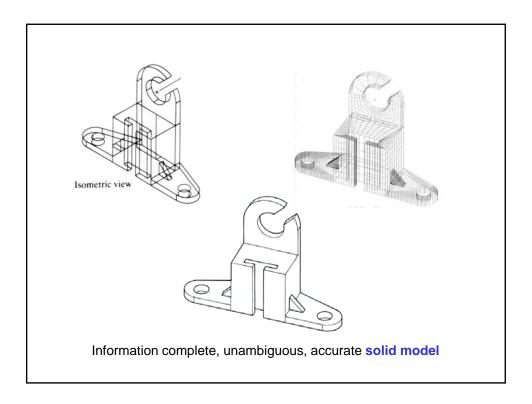
Block: $\{(x, y, z) : 0 < x < W, 0 < y < H, and 0 < z < D\}$

Cylinder: $\{(x, y, z) : x^2 + y^2 < R^2, \text{ and } 0 < z < H\}$



Different Solid Modeling Techniques

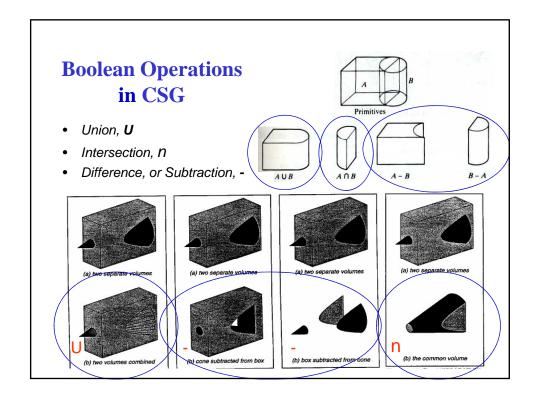
- Constructive Solid Geometry (CSG)
- Sweeping
- Boundary Representation (B-Rep)
- Feature-Based Modeling uses feature-based primitives to conduct a design
- Primitive Instancing uses large numbers (200 300) of "primitives" to build object - used for programming NC machine tools (past)
- Cell Decomposition, Spatial Enumeration, Octree (connected cubes of varying size) – used for irregular objects, image processing, medical applications (CT)

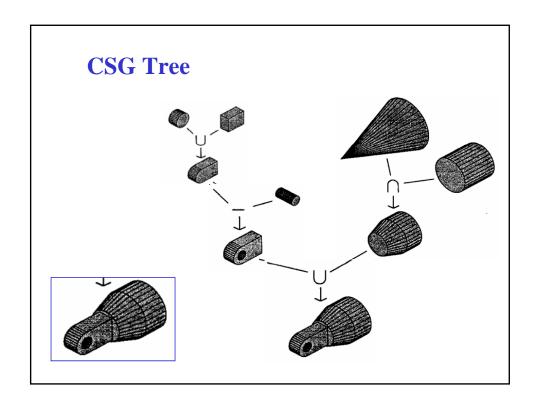


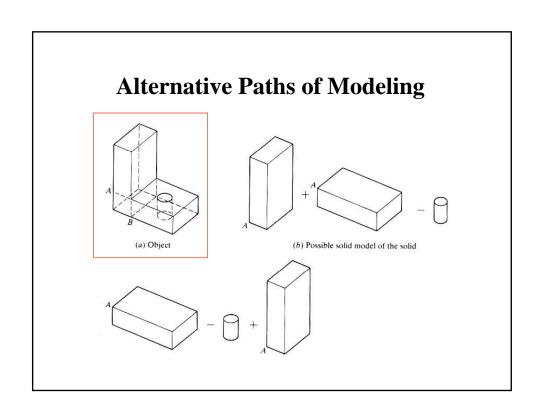
Constructive Solid Geometry (CSG)

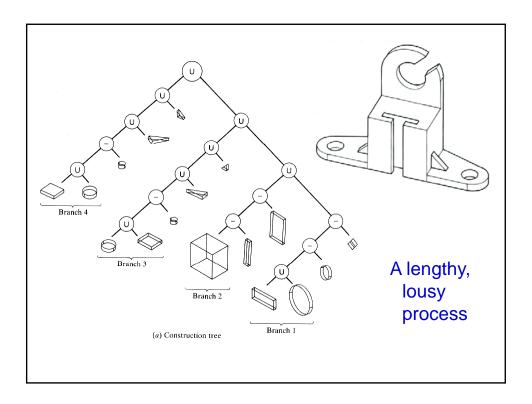
- Pre-defined geometric primitives
- Boolean operations
- CSG tree structure (building process/approach)

• A collection of pre-defined (low level) geometric primitives • Sweeping of a 2D cross-section in the form of extrusion and revolving are used to define the 3D shape (for uncommon shapes). Low Level Geometric Primitives Defined Geometric Features









Sweeping

Sweeping can be carried out in two different forms:

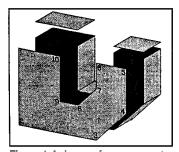
- Extrusion to produce an object model from a 2D cross-section shape, the direction of extrusion, and a given depth. Advanced applications include curved extrusion guideline and varying cross-sections.
- Revolving to produce a rotation part, either in solid or in shell shape. Revolving a 2D cross-section that is specified by a closed curve around the axis of symmetry forms the model of an axially symmetric object.

Sweeping is most convenient for solids with <u>translational</u> or <u>rotational</u> symmetry. Sweeping also has the capability to guarantee a <u>closed</u> object.

Advanced: spatial sweeping; & varying cross-section

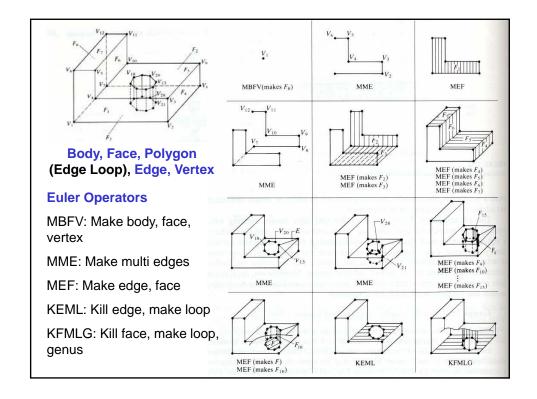
Boundary Representation (B-rep)

- The boundary representation method represents a solid as a collection of boundary surfaces.
 The database records both of the surface geometry and the topological relations among these surfaces.
- Boundary representation does not guarantee that a group of boundary surfaces (often polygons) form a closed solid. The data are also not in the ideal form for model calculations.
- This representation is used mainly for graphical displays.
- Many CAD systems have a hybrid data structure, using both CSG and B-rep at the same time (i.e. Pro/E).



Boundary Representation (B-rep)

- Object List ---- giving object name, a list of all its <u>boundary</u> surfaces, and the relation to other objects of the model.
- **Surface List** ---- giving surface name, a list of all its <u>component</u> <u>polygons</u>, and the relation to other <u>surfaces</u> of the object.
- Polygon List ---- giving polygon name, a list of all <u>boundary</u> <u>segments</u> that form this polygon, and the relation to other <u>polygons</u> of the surface.
- Boundary List ---- giving boundary name, a list of all <u>line</u> segments that for this boundary, and the relation to other boundary lines of the polygon.
- Line List ---- giving line name, the name of its two end points, and the relation to other lines of the boundary line.
- Point List --- giving point name, the X, Y and Z <u>coordinates</u> of the point and, and the relation to other end point of the line.



Feature-based, Parametric Models – Pro/E

- Feature-based, Parametric Solid Modeling system represents the recent advance of computer geometric modeling. It is used as the foundation of Pro/ENGINEER, etc.
- Feature-based, parametric solid modeling eliminated the direct use of common geometric primitives such as cone, cylinder, sphere, etc, since these primitives only represent low-level geometric entities. In designing and manufacturing mechanical parts, one would always refer to mechanical features.
- The modeling approach uses sweeping to form the main shape of the part, and build-in mechanical features to specify the detailed geometry of the model. These features include holes (through, blind, sink), rounds, chamfers, slots, etc. Operations to solid model, such as cut and shell (change a solid model into a hollow shell) are also supported.
- To create the 2D cross-section for *sweeping*, a 2D sketch needs to be generated in the **2D Sketcher**. A user can sketch the rough shape of the closed shape. The system will automatically assign a dimension value of the sketched feature. The **dimensions** of the sketched feature can be changed at any time by simply entering the desired <u>value</u>, or kept as a <u>variable</u>, allowing even more convenient change of its value. The user has to provide all necessary dimensions to pass the section of cross-section generation. Problems of under- or over- dimensioning can be identified.

Pro/E Model Generation

Introducing Datum Primary Shape Definition

- Drawing Rough 2D Cross-section in A 2D Sketcher
- Defining the Precise Geometry
- Building Solid Objects
 - Extrusion to Form Depth
 - Revolving to Form Rotational Features
 - Sweeps and Blends

Adding Detailed Geometry

- Making Holes and Cuts
- Adding Rounds, Chamfers, Slots, and Shells

Summary - Geometric Modeling

- Geometric Modeling is a <u>fundamental</u> CAD technique.
- The capability of various <u>CAD tools</u> in <u>geometric modeling</u> is usually used as a crucial factor in tool selection.
- Wireframe models consist entirely of points, lines, and curves.
 - Since wireframe models do not have "body knowledge", topological data are not needed in construction.
- Surface models store topological information of their corresponding objects.
 - Both surface models and solid models support shading. Surface models is still ambiguous and thus cannot support a full range of engineering activities such as stress analysis.
- Solid models have <u>complete</u>, valid and unambiguous spatial addressability.
 - In general, a wireframe model can be extracted from a surface or a solid model.

Wireframe Modeling

Advantages

- Simple to construct
- Does not require as much as computer time and memory as does surface or solid modeling (manufacturing display)
- As a natural extension of drafting, it does not require extensive training of users.
- Form the basis for surface modeling as most surface algorithms require wireframe entities (such as points, lines and curves)

Disadvantages

- The input time is substantial and increases rapidly with the complexity of the object
- Both topological and geometric data need to be user-input;
 while solid modeling requires only the input of geometric data.
- Unless the object is two-and-a-half dimensional, volume and mass properties, NC tool path generation, cross-sectioning, and interference cannot be calculated.

Surface Modeling

Advantages:

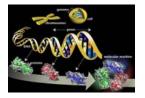
- Less ambiguous
- Provide hidden line and surface algorithms to add realism to the displayed geometry
- Support shading
- Support volume and mass calculation, finite element modeling, NC path generation, cross sectioning, and interference detection. (when complete)

Disadvantages

- Require more <u>training and mathematical background</u> of the users
- Require more CPU time and memory
- Still <u>ambiguous</u>; <u>no topological</u> information
- Awkward to construct

CSG and Brep

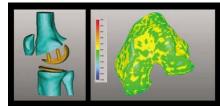
- 1. CSG uses Euler operators in modeling.
- 2. CSG needs low storage due to the simple tree structure and primitives.
- 3. CSG primitives are constructed from the <u>half-space</u> concept.
- 4. <u>Directed surfaces, Euler operations and Euler's law</u> fundamentally distinguish the B-rep from wireframe modeling.
- Traditionally, CSG cannot model <u>sculptured</u> objects and thus is limited in modeling capability. (This is no longer true for Adv. CAD systems, such as Pro/E)
- 6. It is easier to convert a CSG model to a wireframe model than to convert a B-rep model to a wireframe model.
- 7. Because both CSG and B-rep use face direction (half-space or surface normal), they can have a full "body knowledge."
- 8. Generally speaking, most high-end CAD tools have the B-rep (or hybrid) method while most low-end tools rely heavily on the CSG method.



New Challenges to Geometric Modeling

- Modeling Porous Medium
- Modeling Non-homogeneous Materials
 - varying density
 - changing composition
 - multiple phases (solid, liquid)





- Biomedical Applications (geometry, materials, motion and mechanics)
 - Medical Images (surgical operation simulator, training and planning)
 - Computer models from CT scans (quantify motion in actual knees)