Flow tones in a pipeline-cavity system: effect of pipe asymmetry

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Received 15 May 2002; received in revised form 11 October 2002

Abstract

Flow tones in a pipeline-cavity system are characterized in terms of unsteady pressure within the cavity and along the pipe. The reference case corresponds to equal lengths of pipe connected to the inlet and outlet ends of the cavity. Varying degrees of asymmetry of this pipe arrangement are investigated. The asymmetry is achieved by an extension of variable length, which is added to the pipe at the cavity outlet. An extension length as small as a few percent of the acoustic wavelength of the resonant mode can yield a substantial reduction in the pressure amplitude of the flow tone. This amplitude decrease occurs in a similar fashion within both the cavity and the pipe resonator, which indicates that it is a global phenomenon. Furthermore, the decrease of pressure amplitude is closely correlated with a decrease of the \( Q \) (quality)-factor of the predominant spectral component of pressure. At a sufficiently large value of extension length, however, the overall form of the pressure spectrum recovers to the form that exists at zero length of the extension.

Further insight is provided by variation of the inflow velocity at selected values of extension length. Irrespective of its value, both the magnitude and frequency of the peak pressure exhibit a sequence of resonant-like states. Moreover, the maximum attainable magnitude of the peak pressure decreases with increasing extension length.

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1. Introduction

Flow through a pipeline-cavity system represents a generic configuration occurring in a wide variety of applications. Due to the separation of flow along the cavity, the potential exists for coupling between the inherent instability mode of the cavity shear layer and an acoustic mode of the pipeline-cavity system. Even when the inflow to the cavity is fully turbulent, and the acoustic wavelength is much longer than the cavity length, pronounced flow tones can occur (Rockwell et al., 2001). In their investigation, the pipes on either side of the cavity were of the same length and oscillations tended to occur only for the even acoustic modes of the pipeline-cavity system.

Flow tones in a pipeline-cavity system are expected to have certain features in common with tones generated by jet excitation of a long organ pipe (Cremer and Ising, 1967; Fletcher, 1979), jet flow through sequential orifice plates (Wilson et al., 1971; Flatau and Van Moorham, 1990; Hourigan et al., 1990), the wake from a flat plate in a test section (Parker, 1966; Cumpsty and Whitehead, 1971; Stoneman et al., 1988), a shear layer past a cavity resonator (DeMetz and Farabee, 1977; Elder, 1978; Elder et al., 1982; Nelson et al., 1981, 1983), and a cavity shear layer adjacent to a side branch duct/pipe (Pollack, 1980; Bruggeman et al., 1989, 1991; Ziada and Bühlmann, 1992; Kriesels et al., 1995; and

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doi:10.1016/S0889-9746(02)00159-7
Ziada and Shine, 1999). Selected features of these extensive investigations over the past three decades are briefly summarized by Rockwell et al. (2001).

Directly pertinent to the present work are the tones arising in a pipeline-cavity system, which includes the case where the pipe actually protrudes into the cavity. These investigations were carried out at the University of Southampton and are described in a series of investigations, which extend from Davies (1981) to Davies (1996a,b). Pressure spectra showed a number of pronounced peaks, which indicated the generation of flow tones. For the case of a long pipe terminated by an axisymmetric cavity, Rockwell and Schachenmann (1982, 1983) employed linearized, inviscid stability theory to determine the phase shifts and amplitude spikes across the shear layer and, in addition, characterized the overall phase difference through the cavity during the generation of locked-on flow tones. Rockwell and Karadogan (1982) employed zero-crossing statistics, along with recursive digital filtering, to determine the degree of phase fluctuation of the organized oscillations of turbulent flow through the cavity.

For the configuration of the pipeline-cavity arrangement, which was investigated by Rockwell et al. (2001), the effect of asymmetry, i.e., different lengths of the pipes attached to the inlet and outlet of the cavity, has not been addressed. The following issues therefore remain unclarified:

(i) For the symmetrical pipeline-cavity system, flow tones occur only for even numbered acoustic modes of the pipeline-cavity resonator. This observation suggests that the occurrence of a pressure node, i.e., a velocity antinode, at the location of the cavity is an essential condition for the generation of a locked-on flow tone. A small asymmetry of the pipe arrangement, which corresponds to different lengths of the pipes at the inlet and outlet of the cavity, may effectively detune the locked-on flow tone by shifting the location of the pressure node. The possibility of a substantial reduction in pressure amplitude with a small extension of, for example, the outlet pipe has not been addressed.

(ii) If a substantial reduction in the pressure amplitude can be attained, the issue arises as to whether it occurs for a pipe extension length that is a small fraction of the acoustic wavelength of the resonant mode.

(iii) The consequence of variation of the inflow velocity at a given length of the pipe extension has remained unexplored. The possibility of generation of a sequence of resonant-like states of the magnitude and frequency of the peak pressure amplitude has not been pursued.

(iv) The occurrence of locked-on flow tones is represented by a sharp peak in the pressure spectrum. The effect of the pipe extension on the shape of this peak, more explicitly its quality (Q)-factor, has not been addressed.

(v) For all of the foregoing variations of the peak pressure amplitude, the degree to which they occur globally, i.e., simultaneously at locations within the cavity and within the pipe resonator, has not been addressed.

2. Experimental system and techniques

Complete details of the experimental system are described by Rockwell et al. (2001). Only the essential features are described herein.

Air was supplied from an air compressor, through air treatment and accumulation facilities, located in a separate room, and isolated from the pipeline-cavity system. An inlet plenum served as a settling chamber at the upstream of the pipeline-cavity system. It was lined with acoustic damping foam and contained a honeycomb arrangement. The main pipeline-cavity arrangement consisted of two 7.87 ft (1 ft = 12 in = 304.8 mm) segments of 1 in inner diameter aluminum pipe. The length of the inlet pipe was selected to ensure that the boundary layer at the leading edge of the cavity was fully developed. One pipe segment was located on the upstream side of the Plexiglas cavity and the other on the downstream side. The pipe asymmetry was achieved by a pipe extension at the exit of the downstream pipe. This extension had an inside diameter of 0.96 in and a wall thickness of 0.02 in. The length of its protrusion from the main pipe was continuously varied from 0 to 24.49 in by using one of the three extension pieces lengths: 4.0, 14.0 and 26.0 in. The pipe asymmetry was achieved by a pipe extension at the exit of the downstream pipe. This observation suggests that the occurrence of a pressure node, i.e., a velocity antinode, at the location of the cavity is an essential condition for the generation of a locked-on flow tone. A small asymmetry of the pipe arrangement, which corresponds to different lengths of the pipes at the inlet and outlet of the cavity, may effectively detune the locked-on flow tone by shifting the location of the pressure node. The possibility of a substantial reduction in pressure amplitude with a small extension of, for example, the outlet pipe has not been addressed.

As indicated in Fig. 1, pressure transducer $p_a$ was located within the pipe upstream of the cavity, and transducers $p_b$ and $p_c$ were positioned within the cavity. High-sensitivity PCB transducers (Model U103A02) were employed. The transducer outputs were connected to a PCB Piezotronic multi-channel signal conditioner, Model 48A. In order to prevent aliasing effects, a low-pass filter was applied to all pressure signals. The signals were then transmitted to a National Instruments board, Model PCI-MIO-16-E-4. This board sampled at a rate of 250,000 samples per second, which is well above the requirements of the present experiment. The acquisition of multiple data was accomplished using a multiplexing technique with a scan interval of approximately 32 ms. A Pentium II 350 MHz computer and...
LabView software were used for processing the transducer signals. During acquisition of data, the sampling rate was set to 4096 samples per second, which resulted in a Nyquist frequency of 2048 Hz. Each of the spectra shown here was obtained by averaging a total of 42 data sets.

3. Effect of variations of length of pipe extension

The three-dimensional plots of Fig. 2 show the magnitude of the pressure peak on a plane of frequency $f$ versus dimensionless pipe extension length $X_T/\lambda$. The acoustic wavelength $\lambda$ is employed as a normalization length. This wavelength is $\lambda = c/f$, in which $c$ is the speed of sound and $f$ is the frequency of the locked-on flow tone for the case $X_T = 0$. The speed of sound corresponding to 21°C and 70% relative humidity is $c = 1,131.53$ ft/s. Therefore, the value of $\lambda$ at the reference frequency of $f = 620$ Hz was found to be 1.80 ft. Each of the three-dimensional plots corresponds to a different location of the pressure transducer. As defined in Fig. 1, pressure $p_a$ is measured in the pipe resonator at a location upstream of the cavity, pressure $p_b$ on the floor of the cavity, and $p_c$ at the impingement corner of the cavity. The data presented in Figs. 2–6 correspond to the constant inflow velocity of 130 ft/s.

Each of the plots of Fig. 2 shows that the initial increase of $X_T/\lambda$ produces a decrease in the pressure amplitude $p$, then at a sufficiently large value of $X_T/\lambda$, the amplitude $p$ again increases. At approximately $X_T/\lambda = 0.5$, the amplitude $p$ nearly recovers to its original value at $X_T/\lambda = 0$. The scale of the pressure amplitude $p_a$ is a factor of 5 smaller than the scales on the plots of $p_b$ and $p_c$, in order to illustrate the similarity in the form of the pressure amplitude response at different locations. The general form of the response is the same at all locations, which indicates that the phenomenon is global. That is, the oscillations of the shear layer along the cavity and the acoustic resonance of the pipeline-cavity system are globally coupled, and attenuation of the pressure amplitude $p$ at one location is necessarily linked to attenuation at other locations as well.

Plan views of the two-dimensional plots are given in Fig. 3. All of these views have a generally similar form. The nominal frequency of interest is the predominant resonant mode at approximately 630 Hz. As the value of $X_T/\lambda$ increases from zero, the pressure amplitude decreases and, correspondingly, the frequency decreases slightly as well. At approximately $X_T/\lambda = 0.25$, the magnitude of $p$ reaches its lowest value, which is evident in both the lower and upper branches of the shaded pattern. Further increases of $X_T/\lambda$ yield an increase in pressure amplitude $p$ along the upper branch until a peak value is again attained at approximately $X_T/\lambda = 0.5$. In fact, this same pattern of pressure
amplitude $p$ occurs for the resonant modes located below and above the mode of interest, which is nominally at 630 Hz. These modes have significantly lower values of pressure amplitude.

The plots of Fig. 4 show the frequency $f_P$, the magnitude $P$ of the peak pressure (normalized by its maximum value $P_{\text{max}}$), and $Q$ (quality)-factor of the pressure peak as a function of length $X_T$ of the pipe extension, which is normalized by the pipe diameter $D$ and the acoustic wavelength $\lambda$. These distributions correspond to pressure transducer $p_u$. They were constructed from the data exhibited in the top plots of Figs. 2 and 3.

The variation of $f_P$ in Fig. 4 shows a maximum decrease of 4% at $X_T/\lambda = 0.25$. This decrease is evident along the lower branch of pressure $p_u$ shown in Fig. 3. It compares with a 6.5% decrease predicted from the simple theoretical relationship $f_n = nc/2L_T$, in which $L_T$ is the total length of the pipeline-cavity resonator with the extension $X_T$. For $X_T/\lambda > 0.25$, the upper branch of $p_u$ in Fig. 3 is considered. The value of $f_P$ in this region is higher than the nominal frequency $f_P = 630$ Hz of the predominant resonant mode. The value of 630 Hz is approached, however, at approximately $X_T/\lambda = 0.5$.
The corresponding variation of the pressure magnitude $P/P_{\text{max}}$ given in the middle plot of Fig. 4, where $P_{\text{max}}$ refers to the maximum value of pressure $P$ observed for the indicated range of $X_T/D$, shows a decrease of two orders of magnitude at $X_T/\lambda \approx 0.25$. A substantial decrease of $P/P_{\text{max}}$ is attainable, however, at a small value of $X_T/\lambda$. For example, $P/P_{\text{max}}$ decreases to approximately one-third its initial value at approximately $X_T/\lambda = 0.05$, which corresponds to $X_T/D = 1.25$ and $X_T/L = 0.5$, in which $L$ is the cavity length and $D$ is the pipe diameter. On the other hand, at $X_T/\lambda \approx 0.5$, the value of $P/P_{\text{max}}$ recovers to a value close to the value at $X_T/\lambda = 0$. A value of $X_T/\lambda = 0.5$ corresponds to an extension of the standing wave pattern by one-half wavelength and recovery of the value of $P/P_{\text{max}}$.

Fig. 3. Plan views of three-dimensional plots of Fig. 2. These views focus on the band of frequencies associated with generation of pronounced peaks of pressure amplitude $p$. 
The corresponding variation of the quality factor $Q$, which is exhibited in the bottom plot of Fig. 4, indicates that changes of $P/P_{\text{max}}$ are directly linked to changes in $Q$. The plot of $Q$ indicates the occurrence of a locked-on flow tone at a zero value of extension, i.e., $X_T/D = X_T/\lambda = 0$, in accord with the findings of Rockwell et al. (2001). In that investigation, values of $Q = 10^3$ corresponded to occurrence of a locked-on flow tone. This value is approximately one order of magnitude larger than the minimum value of $Q$ in the plot of Fig. 4. In fact, the minimum values of $Q \approx 80–100$ are in the general range of the $Q$-factor of the pipeline-cavity system in absence of throughflow, as determined by transient decay from abrupt termination of loudspeaker excitation and steady-state response to broadband loudspeaker excitation. These experiments were performed during a preliminary phase of this research program. This observation suggests that locked-on flow tones do not exist at, and in the vicinity of, $X_T/\lambda = 0.25$.

Actual spectra are shown for selected values of $X_T/D$ in Fig. 5. It should be noted that plots of pressure amplitude versus frequency are referred to as spectra throughout this article. The relation between the values of $X_T/\lambda$ and $X_T/D$ can be obtained by comparison of the horizontal axes of the plots of Fig. 4. At a sufficiently large value of $X_T/D = 1.5$, the peak amplitude of the predominant spectral component becomes substantially smaller and, at $X_T/D = 2.25$, decreases further. Moreover, the peak values of the side modes also decrease. This observation suggests that the effect of the pipe extension $X_T$ is to attenuate both the predominant locked-on mode and the neighboring modes that are
excited by: turbulence within the pipes; and turbulence/instabilities along the shear layer of the cavity. The spectra given in the right column of Fig. 5 show the recovery of the spectral distribution of pressure to approximately its original form for the case of no pipe extension. This recovery is evident from comparison of the spectral distributions at $X_T/D = 0, 9.25$ and 10. Portions of the spectra at $X_T/D = 9.25$ and 10, particularly in the vicinity of 450 and 1000 Hz, do not, however, exhibit the same form as the spectrum at $X_T/D = 0$. Otherwise, the form of the recovered spectrum is quite similar, including occurrence of the first harmonic at approximately 1250 Hz.

Fig. 6 emphasizes the variation in shape of the predominant spectral component of each of the spectra of Fig. 5. For purposes of comparison, the scale on the vertical ordinate of each plot of Fig. 6 is adjusted to produce approximately the same peak amplitude. The increase in width of the spectral peak, which corresponds to a decrease in the value of the $Q$ (quality)-factor, is evident as $X_T/D$ increases from 0 to 2.25. Conversely, decreases in the width of the peak over the range $X_T/D = 7.25$ to 9.25 correspond to increases of the value of $Q$. At $X_T/D = 10$, the width of the spectral peak again decreases, due largely to the uncertainty of the $Q$-factor calculation, which is highly sensitive to the frequency resolution. Nevertheless, the value of $Q$ remains sufficiently high that the tone remains locked on. That is, $Q$ is well above the aforementioned maximum values of $Q \approx 80–100$.

4. Effect of variations of inflow velocity at constant value of pipe extension length

The data described in the foregoing section show the substantial changes in frequency $f_P$, peak amplitude $P/P_{\text{max}}$ and quality factor $Q$ with changes in length of the pipe extension $X_T$ at a given value of inflow velocity $U$. In this section, emphasis is on the variation of the inflow velocity $U$ at selected values of the extension length $X_T$. 

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Fig. 5. Selected spectra of the pressure $p$ as a function of length $X_T$ of the pipe extension normalized by the pipe diameter $D$. 
The three-dimensional plots of Fig. 7 correspond to values of $X_T/D = 0.25$ and 1.5. Note that the vertical scale of the plot at $X_T/D = 0.25$ represents the amplitude of the pressure $p$, has been compressed by a factor of four relative to the vertical scale at $X_T/D = 1.5$. This compression allows direct comparison of the general form of the plots at $X_T/D = 0.25$ and 1.5. It is evident that the overall response of the pressure amplitude $p$ and the frequency $f_P$ with variation of the inflow velocity $U$ is generally similar for both cases, despite the substantially lower magnitudes of $p$ at $X_T/D = 1.5$. In essence, both plots show a similar, stage-like behavior. That is, the oscillation jumps to successively higher resonant modes of the pipeline-cavity system as velocity $U$ increases. Moreover, within each resonant mode, a relatively large value of pressure $p$ is attained; near the jump from one mode to the next, the value of pressure $p$ becomes relatively small.

These features are shown more explicitly in the plots of Fig. 8, which exhibit the peak pressure amplitude $P$ and the corresponding frequency $f_P$ taken from the spectrum at each value of $U$. At values of $X_T/D = 0.25$, 1.0 and 1.5, the values of $P$ occur at approximately the center of each of the resonant modes of the plot of $f_P$, which is exhibited in the right column. In fact, this general tendency is discernible at the largest value of $X_T/D = 2$, even though this is not a case of true lock-on, as is evident from the low values of $P/P_{max}$ and $Q$ shown in the plots of Fig. 4.

Fig. 9 shows the data of Fig. 8 superposed on common axes of $P$ versus $U$ and $f_P$ versus $U$. The legend that defines the symbols for values of $X_T/D$ is valid for both plots. In the top plot, two sets of symbols are filled, in order to allow better distinction between variations of $P$ versus $U$. The maximum values of $P$ shift to lower values of inflow velocity $U$ as $X_T/D$ increases from 0.25 to 1.0. Further increases of $X_T/D$ result in either an increase, or an indiscernible change, of the velocity $U$ at which peaks of $P$ occur. Regarding the frequency $f_P$, the value of $X_T/D$ has a detectable effect on the value of $U$ at which the frequency jumps to the next mode. It varies over the range $131 \leq U \leq 134$ ft/s.
Selected spectra of pressure $p$, which correspond to the data sets of Figs. 8 and 9, are given in Fig. 10. For each spectrum, the values of $X_T/D$ and $U$ are indicated. The criterion for selection of the value of $U$ is as follows. It corresponds to the first peak in each distribution of amplitude $P$ in Fig. 8. The general form of the spectra of Fig. 10 is quite similar. At the largest value of $X_T/D = 2.0$, attenuation of the peak at the predominant component of 680 Hz is accompanied by disappearance of the distinctive first harmonic at 1360 Hz.

Zoomed-in plots of the predominant spectral peaks of Fig. 10 are exhibited in Fig. 11. Note that the vertical ordinate of each plot has been adjusted to provide the same peak amplitude, thereby providing a physical portrayal of the decrease in $Q$-factor with increasing $X_T/D$. As in Fig. 10, each of these zoomed-in plots is taken at the value of velocity $U$ corresponding to the maximum value of the peak pressure amplitude $P$. This observation indicates that, irrespective of the variation of velocity $U$ over a relatively wide range in Figs. 7–9, the maximum value of the $Q$-factor is limited by the value of $X_T/D$. That is, at successively larger values of $X_T/D$, the maximum attainable value of $Q$ decreases.

5. Concluding remarks

Flow through a pipeline-cavity system, where the length of the pipe at the cavity inlet is equal to the length at the outlet, is known to give rise to locked-on flow tones. The present investigation has examined the consequences of a difference in length of the inlet and outlet pipes; this was accomplished using an extension of length $X_T/D$ of the outlet pipe. The effects of this extension are summarized below.
Substantial attenuation of the peak pressure amplitude of a locked-on flow tone occurs when the pipe extension $X_T$ is of the order of a few percent, e.g., 5%, of the acoustic wavelength, $X_T/\lambda = 0.05$. This extension corresponds, however, to approximately one-half the cavity length $L$, i.e., $X_T/L \approx 0.5$.

A reduction in the peak pressure amplitude $P$ is associated with a corresponding decrease of the quality factor $Q$ of the predominant pressure peak, as well as a decrease in the frequency $f_P$ of the spectral component corresponding to the peak pressure. In fact, at sufficiently large values of $X_T/\lambda$, the values of $Q$ are approximately equal to the values obtained for turbulent flow through a pipe in absence of a cavity. This observation indicates that even a marginally locked-on state does not exist in this range.

At a sufficiently large value of the pipe extension, corresponding to $X_T/\lambda \approx 0.5$, the amplitude of the peak pressure $P$, its frequency $f_P$, and the quality factor $Q$ approximately recover to the values obtained for no pipe extension, $X_T/D = 0$. Moreover, the overall form of the pressure spectrum is generally similar at $X_T/\lambda \approx 0.5$ and 0.

Variation of the inflow velocity $U$ at a given value of pipe extension $X_T/\lambda$ yields a sequence of resonant-like states of the peak pressure amplitude. The major features of this sequence of states are successive jumps to higher order modes of the resonant pipeline-cavity system, as well as occurrence of a well-defined maximum of the peak pressure amplitude within each state. This stage-like behavior persists even for larger values of $X_T/\lambda$ for which the

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Fig. 9. Variations of Fig. 8 plotted on the same set of axes.

Fig. 10. Selected spectra of pressure $p$ for the data sets of Figs. 8 and 9. The value of velocity $U$ indicated on each plot corresponds to occurrence of the maximum value of peak amplitude $P$ as $U$ is varied.
peak pressure amplitude is substantially attenuated. In essence, the effect of the pipe extension is to limit the value of peak pressure amplitude that can be attained when the inflow velocity $U$ is varied over a substantial range. The overall forms of the pressure amplitude and frequency variations with inflow velocity $U$ are generally similar at different values of $X_T/\lambda$.

**Acknowledgements**

The authors are grateful for financial support under Office of Naval Research Grant No. N00014-98-1-0817.

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